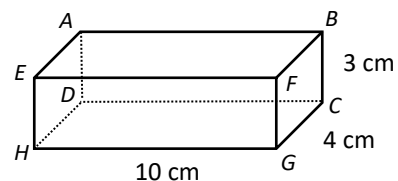
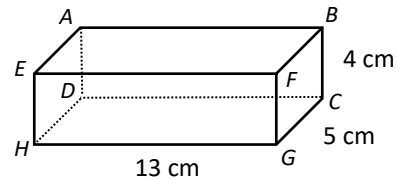
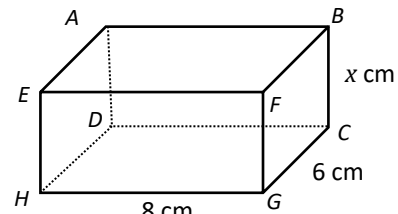
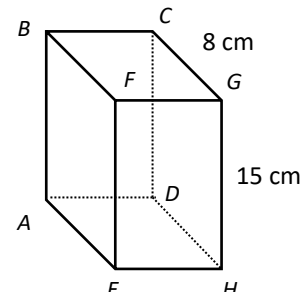
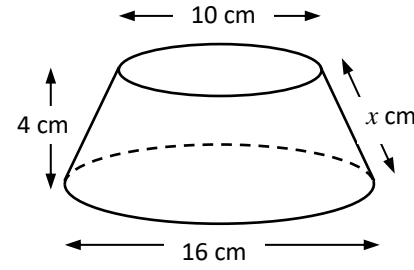
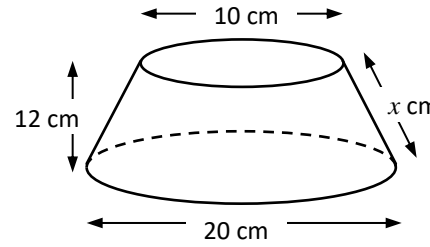
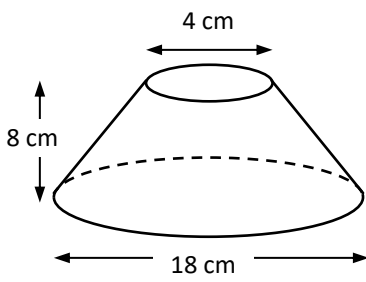
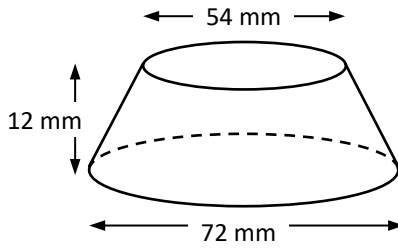


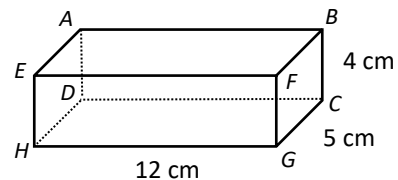
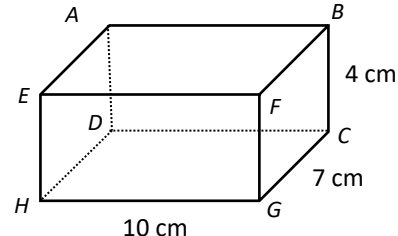
<p>1 Use Pythagoras' theorem to find the length of a given diagonal in a cuboid</p>	
<p>a Calculate the length of AC</p>	
<p>b Jemima is asked to calculate the length of BH. Her answer is 12.6 to 1 decimal place. Do you agree with Jemima? Explain your answer.</p>	

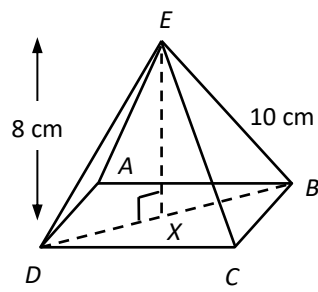
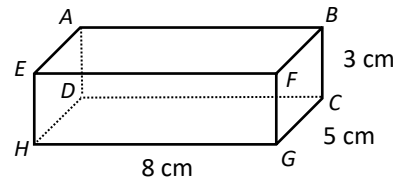
<p>2 Use Pythagoras' theorem to find any length in a cuboid</p>	
<p>a In this cuboid, $BH = 5\sqrt{5}$ Calculate the length of BC</p>	
<p>b In this cuboid, $CE = \sqrt{314}$ Glenn works out the length of FG as follows: $\sqrt{314 - 15^2} = \sqrt{314 - 225} = \sqrt{89}$ Glenn is wrong. Explain why.</p>	

<p>3 Use Pythagoras' theorem to find missing lengths in other three dimensional figures</p>	
<p>a Find the length of x in this frustum of a cone.</p>	
<p>b Miles is asked to find the length of x in this frustum of a cone. He gives the answer 15.6 Do you agree with Miles? Explain why.</p>	

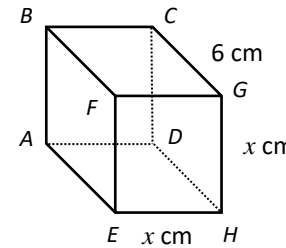
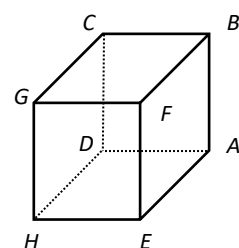


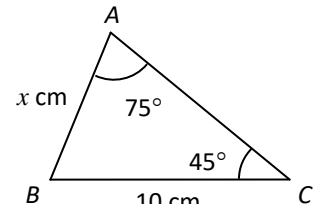
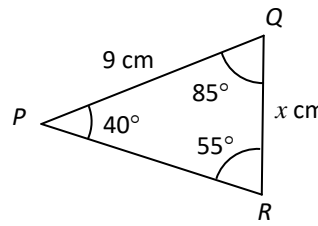
<p>4 Use Pythagoras' theorem to solve problems involving three dimensional figures</p>	
<p>a Find the exact volume of this frustum of a cone.</p>	
<p>b Alison is asked to find the surface area of this frustum of a cone.</p> <p>She works out that the slant height of the frustum is 15 mm. She uses this to find the surface area as follows:</p> $\pi \times 36 \times 60 - \pi \times 27 \times 45 = 2968.80\dots$ <p>Alison is wrong. Explain why.</p>	

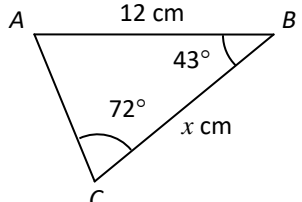
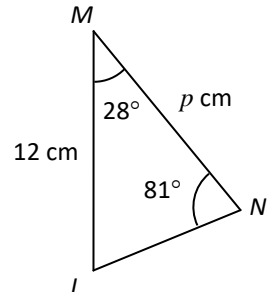
<p>5 Use trigonometry to find the angle between a line and a plane</p>	
<p>a Calculate angle AGD.</p> <p>Give your answer to 1 decimal place.</p>	
<p>b Michael is asked to calculate angle EBH</p> <p>He gives the answer 71.9° to 3 significant figures.</p> <p>Do you agree with Michael? Explain why.</p>	

<p>6 Solve simple problems involving missing lengths and angles in three dimensional figures</p>	
<p>a $ABCD$ is a square X is the midpoint of BD $EX = 8$ cm $BE = 10$ cm</p> <p>Calculate the angle BED. Give your answer to 1 decimal place.</p>	
<p>b Milly is told that angle $AGD = 17.6^\circ$ to 1 decimal place.</p> <p>She works out that $AD = 29.7$ cm</p> <p>Milly is wrong. Explain why.</p>	

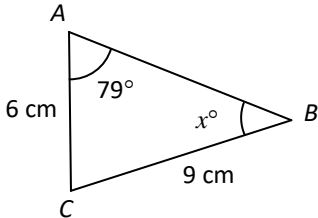
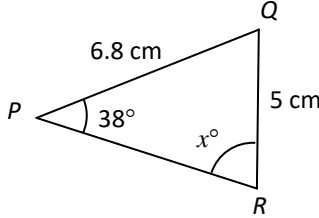


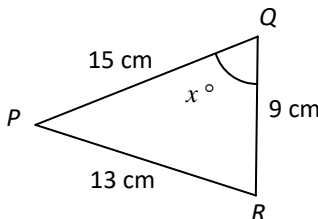
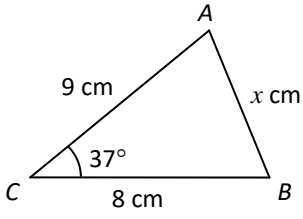
7 Solve more complex problems involving missing lengths and angles in three dimensional figures	
<p>a In this cuboid, angle $AGH = 59^\circ$.</p> <p>Calculate the value of x.</p>	
<p>b $ABCDEFGH$ is a cube.</p> <p>Phil is asked to work out the size of angle ABH. He says,</p> <p><i>'This is not possible as I need to know the length of the sides of the cube'</i></p> <p>Do you agree with Phil? Explain why.</p>	

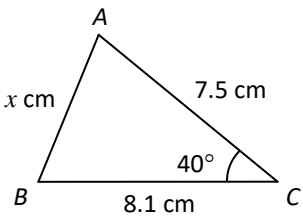
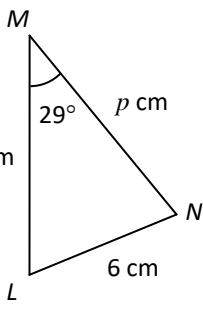
8 Know and use the sine rule in simple cases	
<p>a Calculate the value of x.</p> <p>Give your answer correct to 3 significant figures.</p>	
<p>b Isha is asked to calculate the value of x.</p> <p>She writes</p> $\frac{9}{\sin 55^\circ} = \frac{x}{\sin 85^\circ}$ <p>Isha is wrong. Explain why.</p>	

9 Use the sine rule to find a missing side in a non-right angled triangle	
<p>a Calculate the value of x.</p> <p>Give your answer correct to 3 significant figures.</p>	
<p>b Anton is asked to calculate the value of p. He writes:</p> $\frac{p}{\sin 71^\circ} = \frac{12}{\sin 81^\circ}$ $p = \frac{12 \sin 71^\circ}{\sin 81^\circ}$ $p = \frac{12 \times 71}{81} = 10.5$ <p>Do you agree with Anton? Explain why.</p>	



10 Use the sine rule to find a missing angle(s) in a non-right angled triangle	
<p>a Calculate the value of x.</p> <p>Give your answer correct to 3 significant figures.</p>	
<p>b Jim is asked to calculate the value of x.</p> <p>He gives the answer 2.21.</p> <p>Jim is wrong. Explain why.</p>	

11 Know and use the cosine rule in simple cases	
<p>a Complete the following statement about triangle PQR.</p> $\underline{\quad}^2 = \underline{\quad}^2 + \underline{\quad}^2 - 2 \times \underline{\quad} \times \underline{\quad} \times \cos x^\circ$	
<p>b Vicki is asked to calculate the value of x. She writes</p> $x^2 = 8^2 + 9^2 - 2 \times 8 \times 9 \times \cos 37^\circ$ $x^2 = 64 + 81 - 144 \times \cos 37^\circ$ $x^2 = 64 + 81 - 144 \times \cos 37^\circ$ $x^2 = 1 \times \cos 37^\circ$ <p>Do you agree with Vicki? Explain why.</p>	

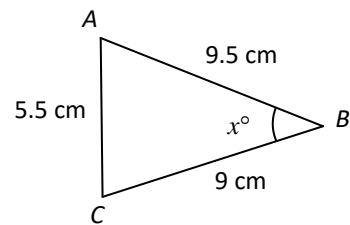
12 Use the cosine rule to find a missing side in a non-right angled triangle	
<p>a Calculate the value of x.</p> <p>Give your answer correct to 3 significant figures.</p>	
<p>b Andy is asked to calculate the value of p. He writes:</p> $p^2 = 6^2 + 12^2 - 2 \times 6 \times 12 \times \cos 29^\circ$ <p>Andy is wrong. Explain why.</p>	



13 Use the cosine rule to find a missing angle in a non-right angled triangle

a Calculate the value of x .

Give your answer correct to 3 significant figures.



b Pat is asked to calculate the value of x . She writes:

$$11^2 = 10^2 + 7^2 - 2 \times 10 \times 7 \times \cos x^\circ$$

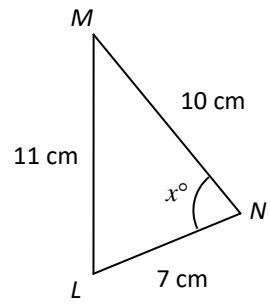
$$121 = 100 + 49 - 140 \times \cos x^\circ$$

$$121 = 9 \times \cos x^\circ$$

$$0.074 \dots = \cos x^\circ$$

$$x = 85.7^\circ$$

Do you agree with Pat? Explain why.



14 Solve complex problems involving bearings

a A boat leaves a port and sails on a bearing of 060° for 200 kilometres. It then turns and sails on a bearing of 160° for 300 kilometres.

The boat then returns directly to the port. What is the distance travelled on the final part of the journey?

Give your answer to the nearest kilometre.

b Jos is given the following problem:

A drone flies on a bearing of 075° for 250 metres. It then turns and flies on a bearing of 135° for 350 metres. The drone then lands. What is the bearing of the drone from its start point?

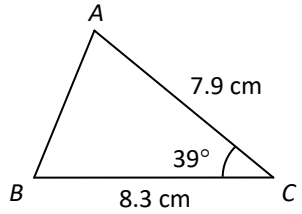
He gives the answer is 070° .

Jos is wrong. Explain why.

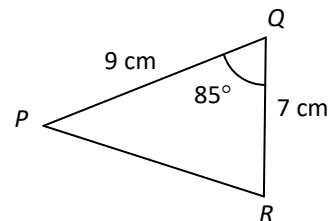
15 Know and use area = $\frac{1}{2}ab \sin C$ to calculate the area of any triangle

a Calculate the area of the triangle ABC .

Give your answer correct to 3 significant figures.

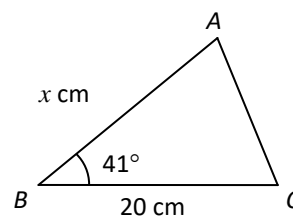



- b** Roy is asked to find the area of triangle PQR .
- He works out the answer -5.55 cm^2 to two decimal places.
- Roy knows he has made a mistake as the answer cannot be negative.
Explain the mistake he has made.



16 Know and use area = $\frac{1}{2}ab \sin C$ to calculate sides or angles of any triangle

- a** The area of triangle ABC is 118 cm^2 .
- Find the value of x .
- Give your answer correct to 3 significant figures.



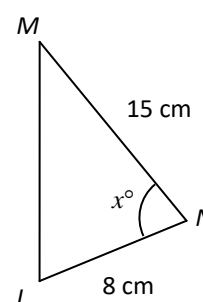
- b** Pete is told that the area of triangle LMN is 59.1 cm^2 .
- He is asked to calculate the value of x . Pete writes:

$$59.1 = \frac{1}{2} \times 8 \times 15 \times \cos x$$

$$0.985 = \cos x$$

$$x = 9.94$$

Do you agree with Pete? Explain why.



	Key learning point	☹	☺	☺	☺
1	Use Pythagoras' theorem to find the length of a given diagonal in a cuboid				
2	Use Pythagoras' theorem to find any length in a cuboid				
3	Use Pythagoras' theorem to find missing lengths in other three dimensional figures				
4	Use Pythagoras' theorem to solve problems involving three dimensional figures				
5	Use trigonometry to find the angle between a line and a plane				
6	Solve simple problems involving missing lengths and angles in three dimensional figures				
7	Solve more complex problems involving missing lengths and angles in three dimensional figures				
8	Know and use the sine rule in simple cases				
9	Use the sine rule to find a missing side in a non-right angled triangle				
10	Use the sine rule to find a missing angle(s) in a non-right angled triangle				
11	Know and use the cosine rule in simple cases				
12	Use the cosine rule to find a missing side in a non-right angled triangle				
13	Use the cosine rule to find a missing angle in a non-right angled triangle				
14	Solve complex problems involving bearings				
15	Know and use $\text{area} = \frac{1}{2}ab \sin C$ to calculate the area of any triangle				
16	Know and use $\text{area} = \frac{1}{2}ab \sin C$ to calculate sides or angles of any triangle				

Top three improvements for me to make



1a	awrt 10.4	
1b	No, she has misused a Pythagorean triple ($CH \neq 12$)	
2a	5	
2b	e.g. the correct answer is 5	
3a	5	
3b	No, the answer is 13	
4a	312π	
4b	She has not included the circular faces	
5a	awrt 17.1°	
5b	No, this is angle EHB	
6a	73.7°	
6b	Correct explanation. $AD = 3$ cm.	
7a	4.5	
7b	No. The answer would be the same for any side length.	
8a	7.32	
8b	$\frac{9}{\sin 55^\circ} = \frac{x}{\sin 40^\circ}$	
9a	11.4	
9b	No, you cannot cancel 'sin'	
10a	40.9	
10b	The correct answer is 56.9	
11a	$13^2 = 9^2 + 15^2 - 2 \times 9 \times 15 \times \cos x^\circ$ or $13^2 = 15^2 + 9^2 - 2 \times 15 \times 9 \times \cos x^\circ$	
11b	Order of operations applied incorrectly	
12a	5.37	
12b	It should be $6^2 = \dots$	
13a	34.5	
13b	Order of operations applied incorrectly	
14a	330 km	
14b	The correct answer is 110° . He has given the bearing of the start point from the current position.	
15a	20.6 cm^2	
15b	The answer is 31.4 (calculator is in radians mode)	
16a	18	
16b	No, he has used 'cos' when it should have been 'sin'	

