## Stage 9: Calculating

It's not quite a quiz, it's not quite a test

| 1 | Calculate with positive indices                           |  |
|---|---|--|
| а | Work out $(2^3 - 5)^4$                                    |  |
| b | Fred is working out $(10 - 2^4)^2$ .                      |  |
|   | He writes $(10 - 2^4)^2$<br>= $(10 - 16)^2$<br>= $-6^2$   |  |
|   | = -36<br>Fred is wrong. Describe the mistake he has made. |  |

| 2 | Calculate with roots   |  |
|---|--|--|
| а | Evaluate $\sqrt[4]{1.5 \times 4 + 10}$                           |  |
| b | Fiona is asked to work out $\sqrt[3]{2 \times 5 + 6 \times 9}$ . |  |
|   | She writes $\sqrt[3]{2 \times 5 + 6 \times 9}$                   |  |
|   | $=\sqrt[3]{10+54}$   |  |
|   | $=\sqrt[3]{64}$  |  |
|   | = 8  |  |
|   | Fiona is wrong. Describe the mistake she has made.               |  |

| 3 | Calculate with negative indices in the context of standard form   |  |
|---|---|--|
| а | Work out $3 \times 10^{-2} \times 8 \times 10^{-1}$ . Give your answer in standard form.  |  |
| b | Faisal is working out $9.6 \times 10^{-3} \div 2.4 \times 10^{-7}$ .  |  |
|   | He writes:<br>$9.6 \div 2.4 = 4$ and $10^{-3} \div 10^{-7} = 10^{-10}$<br>So $9.6 \times 10^{-3} \div 2.4 \times 10^{-7} = 4 \times 10^{-10}$ |  |
|   | Do you agree with Faisal? Explain why.  |  |

| 4 | Use a calculator to evaluate numerical expressions involving powers |  |
|---|---|--|
| а | Use your calculator to evaluate                                     |  |
|   | $\left(\frac{3+2\times4.5}{7}\right)^3$                             |  |
|   | Give your answer as a fraction.                                     |  |
| b | Ffion uses her calculator to work out $(63 - 5.3 \times 2.1^3)^4$ . |  |
|   | She writes the answer 37509.82701 .                                 |  |
|   | Do you agree?   |  |

5 Use a calculator to evaluate numerical expressions involving roots

**a** Use your calculator to work out

$$\sqrt[7]{(1+19) \times 75}$$

Give your answer correct to three significant figures.

**b** Frank uses his calculator to work out  $\sqrt[3]{4.1 + 2.3 \div 1.15}$ .

He writes the answer 7.41 to two decimal places.

Do you agree?

6 Add numbers written in standard form

**a** Evaluate  $2.45 \times 10^6 + 7.3 \times 10^5$ . Give your answer in standard form.

Fran is working out  $1.23 \times 10^{-3} + 4.5 \times 10^{-2}$ .

She writes:

b

 $1.23 \times 10^{-3} = 0.00123$  and  $4.5 \times 10^{-2} = 0.045$ 

and 0.00123 + 0.045 = 0.00573

Fran is wrong. Explain why.

| 7 | Subtract numbers written in standard form                                       |  |
|---|---|--|
| а | Work out $6 \times 10^4 - 4.2 \times 10^3$ . Give your answer in standard form. |  |
| b | Fabian evaluates $7.3 	imes 10^7 - 1.1 	imes 10^3$                              |  |
|   | His answer is $6.2 	imes 10^4$  |  |
|   | Do you agree with Fabian? Explain why.  |  |

| 8 | Multiply numbers written in standard form  |  |
|---|--|--|
| а | Evaluate $4.8 \times 10^4 \times 5 \times 10^6$ . Give your answer as an ordinary number.                      |  |
| b | Felicity is asked to work out $5 \times 10^{-3} \times 4 \times 10^{-2}$ and give her answer in standard form. |  |
|   | Her answer is $20 	imes 10^{-5}$ .   |  |
|   | Felicity is wrong. Explain why.  |  |

| 9 | Divide numbers written in standard form  |  |
|---|--|--|
| а | Work out $3 \times 10^{-3} \div 5 \times 10^{-5}$ . Give your answer as an ordinary number.          |  |
| b | Fergus is asked to work out $3 \times 10^6 \div 6 \times 10^4$ and give his answer in standard form. |  |
|   | Fergus writes the answer $0.5	imes 10^2$ .   |  |
|   | Do you agree with Fergus? Explain why.   |  |



| 10 | Use standard form on a scientific calculator including interpreting the standard form display of a scientific calculator |  |
|----|--|--|
| а  | The volume of the planet Neptune is $6.25 \times 10^{13} \text{ km}^3$ .   |  |
|    | The volume of planet Earth is 57.7 times less than Neptune.  |  |
|    | Work out the volume of Earth. Write your answer in standard form.  |  |
| b  | Fenella uses her calculator to work out $\ 3.2 	imes 10^{21} \div 8.79 	imes 10^{-5}$ .                                  |  |
|    | She writes down the answer $3.64 \times 10^{25}$ .   |  |
|    | Do you agree? Explain why.   |  |

## 11 Understand the difference between truncating and rounding

Is the following statement always true, sometimes true, or never true? Justify your decision.

'Truncating a number to one decimal place gives the same result as rounding to one decimal place'

**b** Fraser writes

а

2.71828 = 2.71 to three significant figures

Fraser is wrong. Explain why.

| 12 | Identify the minimum and maximum values of an amount that has been rounded (to nearest x, x d.p., x s.f.)                                |  |  |
|----|--|--|--|
| а  | The most viewed TV programme on Christmas Day, 2018 was the Queen's Speech. 6.4 million people watched this programme.                   |  |  |
|    | 6.4 million has been rounded to two significant figures. What is the minimum number of people who could have watched the Queen's speech? |  |  |
| b  | A measurement is given as 152 cm to the nearest centimetre.  |  |  |
|    | Faith thinks that the maximum value of the measurement is 152.4 cm.  |  |  |
|    | Do you agree with Faith? Explain why.  |  |  |

| 13 | Use inequalities to describe the range of values for a rounded value                               |  |
|----|--|--|
| а  | The geometry chart for a bike gives the measurement HA = $68^{\circ}$ to the nearest whole number. |  |
|    | Complete this statement to show the range of possible values for HA.                               |  |
|    | ≤ HA <   |  |
| b  | A sack of compost weighs 20 kg to the nearest kilogram. Fergal writes                              |  |
|    | $19.5 \le mass of compost (kg) < 20.499$   |  |
|    | Fergal is wrong. Explain why.  |  |

| 14 | Solve problems involving the maximum and minimum values of an amount that has been rounded |                          |  |
|----|--|--------------------------|--|
| а  | The length and width of a rectangular field have been measured to the nearest metre.       | 156 m                    |  |
|    | Work out the <b>greatest possible value</b> of the area of the field. 68 m                 |                          |  |
| b  | Two angles in a triangle are measured as 48° and 63°. Both measurements are give           | n to the nearest degree. |  |
|    | Freda is asked to work out the greatest possible value of the third angle? She write       | 25                       |  |
|    | $180^{\circ} - 48.5^{\circ} - 63.5^{\circ} = 68^{\circ}$                                   |                          |  |
|    | Freda is wrong. Explain why.   |                          |  |

## Stage 9: Calculating

|    | Key learning point   | 8 |  | $\odot$ |
|----|--|---|--|---------|
| 1  | Calculate with positive indices  |   |  |         |
| 2  | Calculate with roots   |   |  |         |
| 3  | Calculate with negative indices in the context of standard form  |   |  |         |
| 4  | Use a calculator to evaluate numerical expressions involving powers  |   |  |         |
| 5  | Use a calculator to evaluate numerical expressions involving roots   |   |  |         |
| 6  | Add numbers written in standard form   |   |  |         |
| 7  | Subtract numbers written in standard form  |   |  |         |
| 8  | Multiply numbers written in standard form  |   |  |         |
| 9  | Divide numbers written in standard form  |   |  |         |
| 10 | Use standard form on a scientific calculator including interpreting the standard form display of a scientific calculator |   |  |         |
| 11 | Understand the difference between truncating and rounding  |   |  |         |
| 12 | Identify the minimum and maximum values of an amount that has been rounded (to nearest x, x d.p., x s.f.)                |   |  |         |
| 13 | Use inequalities to describe the range of values for a rounded value   |   |  |         |
| 14 | Solve problems involving the maximum and minimum values of an amount that has been rounded                               |   |  |         |

Top three improvements for me to make



## Stage 9: Calculating

| 1a  | 81  |  |
|-----|---|--|
| 1b  | It should be $(-6)^2 = 36$  |  |
| 2a  | 2   |  |
| 2b  | She has found the square root of 64. The cube root of 64 is 4.                      |  |
| 3a  | $2.4 \times 10^{-2}$  |  |
| 3b  | No, and reason; e.g. $10^{-3} \div 10^{-7} = 10^4$                                  |  |
| 4a  | $\frac{1728}{343}$  |  |
| 4b  | Yes   |  |
| 5a  | 2.84  |  |
| 5b  | No, it should be 1.827 (Frank has done 3×, instead of the cube root)                |  |
| 6a  | $3.18 \times 10^{6}$  |  |
| 6b  | e.g. the answer should be 0.04623   |  |
| 7a  | $5.58 \times 10^4$  |  |
| 7b  | No, and reason; e.g. the answer is 72 998 900                                       |  |
| 8a  | $2.4 \times 10^{11}$  |  |
| 8b  | Not in standard form  |  |
| 9a  | 60  |  |
| 9b  | Not in standard form  |  |
| 10a | $1.08 \times 10^{12}$ (3sf)   |  |
| 10b | Yes, she has rounded to two decimal places (for example)                            |  |
| 11a | Sometimes true  |  |
| 11b | He has truncated  |  |
| 12a | 6.35 million  |  |
| 12b | No, and reason; e.g. 152.43 is bigger   |  |
| 13a | $67.5^{\circ} < HA \le 68.5^{\circ}$  |  |
| 13b | The upper limit should be 12.5  |  |
| 14a | 10720.25 m <sup>2</sup>   |  |
| 14b | She should have worked out $180^{\circ} - 47.5^{\circ} - 62.5^{\circ} = 70^{\circ}$ |  |